Abstract. This paper studies a decode-and-forward (DF) full-duplex cooperative relaying network, whereas one transmitter S transmits information to one receiver D via the help of a relay R. In particular, the transmitter can simultaneously transmit energy and information (SWIPT) to relay R using time-switching (TS) method. Then, relay R can utilize the harvested energy to transfer information to the receiver D. Based on the proposed system model, we derive the mathematical expressions for the system capacity for the proposed non-adaptive TS (NATSP) and adaptive TS protocols (ATSP). Next, the Monte Carlo simulations are executed to corroborate the exactness of the analysis compared to the numerical results. Both numerical and analytical results show the superiority of ATSP over NATSP.

Keywords


1. Introduction

Recently, the Internet of things (IoT) has received great attention from both industrial and academic because of its important role in the fifth generation (5G) and beyond [1–6]. The work in [1] investigated the performance of the cognitive IoTs networks by employing multiple relays via a deep learning approach. It, however, focuses on outage probability rather than the ergodic capacity. Authors in [2] also applied artificial intelligence (AI) to address the security issue in energy harvesting-enabled IoT networks. The backscatter-assisted mobile edge computing in IoTs networks was studied in [3]. Particularly, by optimizing the transmit power at the gateway, the time-switching ratio of the sum rate is maximized. Liu and others in [4] also maximized the transmission rate under the constraint of total transmit power and resource allocations. These works, however, rely on the numerical approach to obtain the optimal solution rather than based on the rigorous mathematical framework. On the other hand, resource allocation in the unmanned aerial vehicle (UAV)
was investigated in [6]. Nonetheless, they do not take into account energy harvested at UAV.

Besides the great benefits of IoT, the enormous number of IoT devices imposes many challenges in communications due to limitations of resources, i.e., available frequency. Owing to the development of self-interference cancellation (SIC) techniques that can obtain a high SI cancellation, full-duplex (FD) is a potential technique to improve the spectrum efficiency by its capability of transmitting and receiving signals at the same time [7, 8]. Due to the above-mentioned advantages, FD has been widely investigated in cooperative relay networks [9–11].

Besides the restriction on the spectrum, IoT devices are usually equipped with limited energy capacity. Battery replacement/recharging is not always convenient or even impossible. Furthermore, the significant increase in resource-intensive IoT applications such as augmented reality (AR), multi-view video construction, and reality (VR) puts more demands on energy consumption and can significantly reduce equipment’s lifetime. Thanks to the development of energy harvesting (EH) techniques, it can become a promising solution to overcome the energy problem of IoT devices. Especially, radio frequency (RF) EH has received great interest due to its controllability and predictability as compared with other ambient resources such as wind [12, 13], solar [14], or water [15]. Consequently, RF EH has been intensively investigated in cooperative relay communications [16–18]. Indeed, RF EH can be divided into two types, termed wireless power transfer (WPT) [16–18] and simultaneous wireless information and power transfer (SWIPT). The main difference between WPT and SWIPT is that the RF signal only carries energy in WPT while it can contain both energy and information in the SWIPT technique.

Motivated by the above discussions, this paper studied the system capacity analysis of a SWIPT- and FD-aided cooperative relay network. Besides, the relay node is equipped with an EH circuit, and it can harvest energy from a transmitter’s RF signals. The contributions of this paper are summarized as follows:

- We investigated and proposed a SWIPT- and FD-aided relay network with one transmitter, one FD relay, and one receiver.
- By considering the above system model, we proposed two protocols, namely, non-adaptive time-switching (NATSP) and adaptive time-switching protocols (ATSP). Besides, we derive the mathematical expression for the system capacity corresponding to each protocol.
- Then, the mathematical results are confirmed through Monte Carlo simulations.

This paper is organized as follows. In Section 2, the system model of the SWIPT- and FD-assisted relay network is described in detail. Then, the system capacity is analyzed in Section 3. The simulation results to validate our analysis are presented in Section 4. Finally, Section 5 concludes the paper.

2. System Model

![System model](image1)

**Fig. 1:** System model.

![Energy Harvesting and Information transmission processing](image2)

**Fig. 2:** Energy Harvesting and Information transmission processing.
As shown in Fig. 1, a transmitter S can transmit both information and energy to a relay R. Moreover, relay R is equipped with an energy harvester circuit, and it can harvest energy from the transmitter’s RF signals. The transmitter S and receiver D operate at half-duplex mode, while relay R can operate at full-duplex mode. The energy harvesting and information transmission of our system are presented in Fig. 2. More specifically, relay R harvested energy during the first time slot $\alpha T$ and transmits data to receiver D during the second time slot $(1 - \alpha)T$. The channels between any two users are assumed to follow block Rayleigh fading. Thus, the squared amplitudes of the channel gains such as $|h_{SR}|^2$, $|h_{RR}|^2$, etc. are exponential random variables (RVs) whose cumulative distribution function (CDF) and probability density function (PDF) have the following forms, respectively:

$$F_{|h_i|^2}(x) = 1 - \exp (-\lambda_i x), \quad (1)$$

$$f_{|h_i|^2}(x) = \lambda_i \exp (-\lambda_i x). \quad (2)$$

where $i \in \{SR, RD, RR\}$ and $\lambda_i$ is the mean of random variables (RVs) $|h_i|^2$, respectively.

From Fig. 1, the received signal at the relay can be expressed by

$$y_R = h_{SR}x_S + h_{RR}x_R + n_R, \quad (3)$$

where $x_S$ is the S’s signal with $E\{ |x_s|^2 \} = P_s$; $x_R$ is the self-interference at R due to full-duplex relaying and satisfies $E\{ |x_R|^2 \} = P_R$, where $E\{ \cdot \}$ denotes the expectation operation; $n_R$ is the additive white Gaussian noise (AWGN) at R. The harvested energy at R during the first time slot can be computed by

$$E_R = \eta \alpha T P_s |h_{SR}|^2, \quad (4)$$

By applying the time-switching (TS) scheme, the average transmit power at R can be thus obtained as [19]

$$P_R = \frac{E_R}{(1 - \alpha)T} = \frac{\eta \alpha P_s |h_{SR}|^2}{(1 - \alpha)} = \mu P_s |h_{SR}|^2, \quad (5)$$

where $0 < \eta \leq 1$ is the energy conversion efficiency and $\mu \overset{\Delta}{=} \eta \alpha / (1 - \alpha)$.

Because relay R can perform full-duplex mode, the signal to interference noise (SINR) at the relay R can be given by

$$\gamma_R = \frac{P_s |h_{SR}|^2}{|h_{RR}|^2 P_R + N_0}. \quad (6)$$

By substituting (5) into (6) and assuming that $N_0 \ll P_s |h_{RR}|^2$, then we have

$$\gamma_R = \frac{P_s |h_{SR}|^2}{\mu P_s |h_{SR}|^2 |h_{RR}|^2 + N_0} \approx \frac{1}{\mu |h_{RR}|^2}. \quad (7)$$

Next, the received signal and SNR at D in the second time slot can be respectively given by

$$y_D = h_{RD}x_R + n_D, \quad (8)$$

$$\gamma_D = \frac{P_R |h_{RD}|^2}{N_0} = \frac{\mu \Psi |h_{SR}|^2 |h_{RD}|^2}{N_0}, \quad (9)$$

where $\Psi = \frac{P_s}{\mu N_0}$ and $n_D$ is the zero mean AWGN with variance $N_0$.

Because we use the decode-and-forward (DF) protocol in our system model. Therefore, the end-to-end SNR and the total received capacity at D can be expressed as, respectively

$$\gamma_{DF} = \min (\gamma_R, \gamma_D), \quad (10)$$

$$C_{DF} = \log_2 (1 + \gamma_{DF}). \quad (11)$$

3. Performance Analysis

3.1. Case 1: Non-adaptive time-switching protocol (NATSP)

The communication capacity of the system can be expressed as [20]

$$C_{DF} = \frac{1}{\ln 2} \int_0^{\infty} \frac{1 - F_{\gamma_{DF}}(x)}{1 + x} dx, \quad (12)$$

From (12), the CDF of $\gamma_{DF}$ is given by

$$F_{\gamma_{DF}}(x) = \Pr (\gamma_{DF} < x) = \Pr (\min (\gamma_R, \gamma_D) < x), \quad (13)$$
In this case, we optimize the time-switching ratio \( \alpha^* \) to maximize the capacity of our proposed system. Because the DF protocol is considered in our work, the \( \alpha^* \) can be obtained by solving the following equation

\[
\gamma_R = \gamma_D \leftrightarrow \frac{1}{\mu |h_{RR}|^2} = \mu |h_{SR}|^2 |h_{RD}|^2
\]

\[
\Rightarrow \mu^2 = \frac{|h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi|}{\eta |h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi + 1|}.
\]

By substituting (19) into (13), the \( F_{\gamma_D}^* \) can be thus expressed by

\[
F_{\gamma_D}^*(x) = \Pr \left( \frac{\sqrt{|h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi|}}{|h_{RR}|^2} < x \right)
\]

\[
= \Pr \left( \frac{|h_{SR}|^2 |h_{RD}|^2}{\mu |h_{RR}|^2} < x \right)
\]

\[
= \Pr \left( \frac{|h_{RR}|^2}{\mu |h_{RR}|^2} < \frac{x}{|h_{SR}|^2} \right.
\]

\[
\approx \int_0^x F_{\mu|h_{RR}|^2} \left( \frac{z |h_{SR}|^2 |h_{RD}|^2}{\mu |h_{RR}|^2} \right) dz.
\]

First, \( P_1 \) in (14) can be calculated by

\[
P_1 = \Pr \left( \frac{1}{\mu |h_{RR}|^2} \geq x \right)
\]

\[
= \Pr \left( |h_{RR}|^2 \leq \frac{1}{\mu x} \right) = 1 - \exp \left( - \frac{\lambda h_{RR}}{\mu x} \right),
\]

where \( X = |h_{SR}|^2 |h_{RD}|^2 \).

By applying (17), equation (20) can be reformulated at the next top of the page.

Let us denote \( t = \sqrt{\eta} \), (21) can be rewritten at the next top of the page.

With the help of [21, Eq. 3.324.1], \( F_{\gamma_D}^* \) can be given by

\[
F_{\gamma_D}^*(x) = 1 - \exp \left( \frac{x^2 |h_{SR}|^2 |h_{RD}|^2}{2 \Psi |\lambda_{RR}|^2} \right) W_{1, -\frac{1}{2}} \left( \frac{x^2 |h_{SR}|^2 |h_{RD}|^2}{\Psi |\lambda_{RR}|^2} \right)
\]

where \( W(\bullet) \) is the Whittaker function.

Finally, the system capacity can be mathematically expressed as

\[
C_{DF}^* = \frac{1}{\ln 2} \left( \frac{1}{x} \right) \exp \left( \frac{x^2 |h_{SR}|^2 |h_{RD}|^2}{2 \Psi |\lambda_{RR}|^2} \right) W_{1, -\frac{1}{2}} \left( \frac{x^2 |h_{SR}|^2 |h_{RD}|^2}{\Psi |\lambda_{RR}|^2} \right) dx.
\]

3.2. Case 2: Adaptive time-switching protocol (ATSP)

In this case, we optimize the time-switching ratio \( \alpha^* \) to maximize the capacity of our proposed system. Because the DF protocol is considered in our work, the \( \alpha^* \) can be obtained by solving the following equation

\[
\gamma_R = \gamma_D \leftrightarrow \frac{1}{\mu |h_{RR}|^2} = \mu |h_{SR}|^2 |h_{RD}|^2
\]

\[
\Rightarrow \mu^2 = \frac{|h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi|}{\eta |h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi + 1|}.
\]

By substituting (19) into (13), the \( F_{\gamma_D}^* \) can be thus expressed by

\[
F_{\gamma_D}^*(x) = \Pr \left( \frac{\sqrt{|h_{RR}|^2 |h_{SR}|^2 |h_{RD}|^2 |\Psi|}}{|h_{RR}|^2} < x \right)
\]

\[
= \Pr \left( \frac{|h_{SR}|^2 |h_{RD}|^2}{\mu |h_{RR}|^2} < x \right)
\]

\[
= \Pr \left( \frac{|h_{RR}|^2}{\mu |h_{RR}|^2} < \frac{x^2}{|h_{SR}|^2} \right)
\]

\[
\approx \int_0^x F_{\mu|h_{RR}|^2} \left( \frac{z^2 |h_{SR}|^2 |h_{RD}|^2}{\mu |h_{RR}|^2} \right) dz.
\]

4. Numerical Results

In this section, we provide the numerical results to corroborate the accuracy of the analysis, i.e., the system capacity. More specifically, the results can be obtained by averaging \( 10^6 \) channel
\[ C_{DF} = \frac{2}{\ln 2} \int_0^\infty \left( 1 - \exp\left( -\frac{\lambda_{RR}}{\mu_{\eta_{th}}} \right) \right) \times \sqrt{\frac{x\lambda_{SR}\lambda_{RD}}{\mu_\Psi}} \times K_1 \left( 2\sqrt{\frac{x\lambda_{SR}\lambda_{RD}}{\mu_\Psi}} \right) \, dx. \quad (18) \]

\[ F^*_\gamma_{DF}(x) = 1 - 2 \int_0^\infty \lambda_{RR} \exp \left( -\lambda_{RR} y \right) \sqrt{\frac{x^2 y \lambda_{SR} \lambda_{RD}}{\Psi}} K_1 \left( 2\sqrt{\frac{x^2 y \lambda_{SR} \lambda_{RD}}{\Psi}} \right) \, dy. \quad (21) \]

\[ F^*_\gamma_{DF}(x) = 1 - 4x\lambda_{RR} \sqrt{\frac{\lambda_{SR} \lambda_{RD}}{\Psi}} \int_0^\infty t^2 \exp \left( -\lambda_{RR} t^2 \right) K_1 \left( 2xt \sqrt{\frac{\lambda_{SR} \lambda_{RD}}{\Psi}} \right) \, dt, \quad (22) \]

**Tab. 1:** Simulation parameters.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Parameter name</th>
<th>Fixed value</th>
<th>Varying range</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \eta )</td>
<td>energy conversion efficiency</td>
<td>0.8</td>
<td>0.05 to 1</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>time switching factor</td>
<td>0.25, 0.355, 0.55, 0.75</td>
<td>0.05 to 0.95</td>
</tr>
<tr>
<td>( \lambda_{SR} )</td>
<td>Parameter of channel power gain (</td>
<td>h_{SR}</td>
<td>^2 )</td>
</tr>
<tr>
<td>( \lambda_{RD} )</td>
<td>Parameter of channel power gain (</td>
<td>h_{RD}</td>
<td>^2 )</td>
</tr>
<tr>
<td>( \lambda_{RR} )</td>
<td>Parameter of SI channel power gain (</td>
<td>h_{RR}</td>
<td>^2 )</td>
</tr>
<tr>
<td>( \Psi )</td>
<td>Transmit power-to-noise-ratio from source</td>
<td>3 dB</td>
<td>-5 to 15 dB</td>
</tr>
</tbody>
</table>

**Fig. 3:** Capacity versus \( \Psi \) (dB) with \( \eta = 0.8 \).

**Fig. 4:** Capacity versus \( \eta \) with \( \Psi = 3(dB) \).
realizations [22–24]. The simulation parameters are listed in Tab. 1.

In Figs. 3 and 4, we sketch the system capacity as a function of $\Psi$(dB) with $\eta = 0.8$ and different $\alpha$ values. It can be observed from Fig. 3 that the larger the $\Psi$ value is, the better the system capacity can be acquired. Moreover, the system capacity is proportional to the $\Psi$ value. It is expected because if we allocate more transmit power to transmitter S, the data transmission rate at receiver D is significantly improved. In particular, when $\Psi < 7$ dB, the system capacity of the NATSP scheme with $\alpha = 0.25$ outperforms the NATSP scheme with $\alpha = 0.75$. Nevertheless, when $\Psi > 7$ dB, the NATSP scheme performance is worse than the NATSP scheme with $\alpha = 0.75$. Moreover, the ATSP performance is always better than that compared to others because it does not depend on $\alpha$ value and it is designed by maximizing the end-to-end SNR at D.

Figure 4 shows the system capacity as a function of energy conversion efficiency $\eta$, where $\Psi = 3$ dB. As can be observed from Fig. 4 that the system performance of the NATSP is greatly increased with the higher value of $\eta$. In addition, the NATSP scheme with $\alpha = 0.355$ can obtain a better capacity compared to the NATSP scheme with $\alpha = 0.55$. Especially, the system capacity of the ATSP scheme is unchanged. It can be explained based on (24) in which the capacity expression does not depend on $\eta$ value.

In Fig. 5, we investigate the effects of the time-switching factor $\alpha$ on the system capacity, with $\eta = 0.8$. The time-switching ratio is crucial because it affects both the time allocation for energy harvesting and information transmission. It can be observed that the system capacity of the NATSP is greatly enhanced when $\alpha$ increases to an optimal point, then it becomes worse. It is because the higher the $\alpha$ value is, the more the allocation time is used for energy harvesting, and less time is used for information transmission. Therefore, there exists an optimal point of $\alpha$ to maximize the system capacity. Similar to Fig. 4, the ATSP obtains a better performance compared to NATSP. However, the capacity of ATSP is unaltered with increasing of $\alpha$. Furthermore, the system capacity is significantly increased when $\Psi$ is from 1 dB to 4 dB.

Figure 6 plots the system capacity as a function of $\lambda_{SR} = \lambda_{RD}$, where $\eta = 0.8$, $\Psi = 3$ dB, and $\lambda_{RR} = 1$. Moreover, the parameter $\lambda_i$ with $i \in \{SR, RR, RD\}$ can be defined as $\lambda_i = (d_i)^\beta$, where $\beta$ is the path loss exponent. Therefore, $\lambda_{SR} = \lambda_{RD}$ implies that the distance between $S \rightarrow R$ equals to the distance between $R \rightarrow D$. It can be seen from Fig. 6 that the system capacity is significantly decreased with a larger distance from source/relay to relay/destination. It can be explained by the fact that the larger the distance is, the more channel attenuation can be obtained. Therefore, it reduces the channel quality, which deteriorates the system’s capacity.

In Fig. 7, the impact of self-interference (SI) level, which represents by the channel parameter $\lambda_{RR}$, on the capacity performance is studied. In this simulation, it is worth noting that higher $\lambda_{RR}$ corresponds to a lower SI level, i.e. better SI cancellation solution due to $1/\lambda_{RR}$ is the mean of SI channel power gain $|h_{RR}|^2$. It can be observed that when the SI level is increased, the capacity is decreased. This can be explained that based on the definition of capacity in equation (12), when the SI level is reduced, $1 - F_{\gamma_{DF}}(x)$ will be increased, hence the capacity will be also increased.
5. Conclusions

This paper studied a cooperative relay network with a transmitter S, a relay R, and a receiver D. Further, the relay user can harvest energy from a transmitter S and use harvested energy to transmit information to D. In particular, the transmitter S can transmit both information and energy to R simultaneously (SWIPT) applying time-switching method. In this context, we derive the system capacity at the receiver for both non-adaptive time-switching (NATSP) and adaptive time-switching protocols (ATSP). The numerical results are presented to validate the correctness of our analysis. The results show the superiority of our proposed ATSP compared to NATSP. The results obtained from this work can motivate interesting future work such as a more generalized model, i.e., Rician or Nakagami-m fading channels.

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References


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